An important aspect of high-performance computing (HPC) system design is the choice of main memory capacity. This choice becomes increasingly important now that 3D-stacked memories are entering the market. Compared with conventional DIMMs, 3D memory chiplets provide better performance and energy efficiency but lower memory capacities. Therefore the adoption of 3D-stacked memories in the HPC domain depends on whether we can find use cases that require much less memory than is available now.

This study analyzes the memory capacity requirements of important HPC benchmarks and applications. We find that the High Performance Conjugate Gradients benchmark could be an important success story for 3D-stacked memories in HPC, but High-performance Linpack is likely to be constrained by 3D memory capacity. The study also emphasizes that the analysis of memory footprints of production HPC applications is complex and that it requires an understanding of application scalability and target category, i.e., whether the users target capability or capacity computing. The results show that most of the HPC applications under study have per-core memory footprints in the range of hundreds of megabytes, but we also detect applications and use cases that require gigabytes per core. Overall, the study identifies the HPC applications and use cases with memory footprints that could be provided by 3D-stacked memory chiplets, making a first step towards adoption of this novel technology in the HPC domain.

CCS Concepts: •Computer systems organization → Distributed architectures; •Hardware → Analysis and design of emerging devices and systems; Memory and dense storage;

Additional Key Words and Phrases: Memory capacity requirements, High-performance computing, Production HPC applications, HPL, HPCG.

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1. INTRODUCTION

Memory systems are important contributors to the deployment and operational costs of large-scale HPC clusters [Kogge et al. 2008; Stevens et al. 2010; Sodani 2011], making memory provisioning one of the most important aspects of HPC system design.\footnote{In our system, the MareNostrum supercomputer [Barcelona Supercomputing Center 2013], main memory accounts to more than 10% of server cost and 10–15% of server energy consumption.} In spite of this, most available analysis guiding memory provisioning is surprisingly ad hoc. Usually large HPC systems follow a rule of thumb that couples 2–3GB of main memory per x86 core or 1 GB per Blue Gene PowerPC core (see Figure 1). It seems that this rule of thumb is based on experience with previous HPC clusters and on undocumented knowledge of the principal system integrators, and it is uncertain whether it matches the memory requirements of production HPC applications.

Even though there are various reports and projections that roughly estimate the memory requirements of existing HPC applications [Atkins et al. 2003; NERSC 2012; 2013; 2014a; 2014b; 2015a; 2015b], there are no or very few studies that thoroughly analyze and quantify the memory footprints of HPC workloads across multiple domains. In this paper we try to bridge this gap and to examine whether current memory design strategies meet the memory requirements of important HPC benchmarks and applications.

In this study, we theoretically analyze and confirm with experimental measurements the memory capacity requirements of High-Performance Linpack (HPL) and High Performance Conjugate Gradients (HPCG), the former being the benchmark used to rank the supercomputers on the TOP500 list. Our measurements show that in current systems achieving good HPL scores requires at least 2 GB of main memory per core, which matches the main memory sizing trends of the large HPC clusters that dominate the TOP500 list. The analysis also shows that, as the total number of cores is increased, more memory per core will be needed to achieve good performance, between 7.6 GB and 16.1 GB in a million-core cluster. In contrast, HPCG memory requirements are fundamentally different. To converge to the optimal performance, the benchmark requires roughly 0.5 GB of memory per core, and this will not change as the cluster size increases.

We also study the memory footprints of the Unified European Application Benchmark Suite (UEABS), large-scale scientific workloads carefully selected to provide good coverage of production HPC applications running on Tier-0 and Tier-1 HPC systems in Europe [PRACE 2013]. We observe a bimodal distribution in memory
requirements, finding that memory requirements depend on application scalability and the targeted HPC category, i.e., whether the workloads represent capability or capacity computing. In HPC, capability computing refers to using large-scale HPC installations to solve a single, highly complex problem in the shortest possible time, while capacity computing refers to optimizing system efficiency to solve as many mid-size or smaller problems as possible at the same time at the lowest possible cost. Based on our findings, we recommend guidelines for selecting an appropriate level of parallelism when designing experiments to quantify memory capacity requirements of production HPC applications. Most of the UEABS applications have per-core memory footprints in the range of hundreds of megabytes — an order of magnitude less than the main memory available in state-of-the-art HPC systems; but we also detect applications and use cases that still require gigabytes of main memory. We also demonstrate that even within the same application, different processes can have memory footprints that vary by an order of magnitude.

To the best of our knowledge, this is the first study that detected and analyzed the dependency between available memory capacity and HPL and HPCG performance. Also, for the first time, we explored the complexity of memory footprint analysis for production HPC applications, and showed how memory footprint depends on application scalability and target HPC category. We hope that this study will motivate the community to question the current trends for memory system sizing in HPC clusters, and will lead to further analysis of memory capacity requirements of HPC systems.

This analysis becomes increasingly important as 3D-stacked memories are hitting the market. Replacing conventional DIMMs with new 3D memory chiplets located on the silicon interposer could be the next breakthrough in memory system design. It would provide significantly higher memory bandwidth and lower latency, leading to higher performance and energy-efficiency. On the down side, however, it is unlikely that (expensive) 3D memory chiplets alone would provide the same memory capacities as DIMM-based memory systems [Sodani et al. 2016]. Therefore the adoption of 3D-stacked memories in the HPC domain depends on whether we can find use cases that require much less memory than is available now.

Academia and industry are also exploring hybrid memory systems that combine 3D-stacked DRAM with standard DIMMs [Dong et al. 2010; Chou et al. 2014; Sim et al. 2014; Meswani et al. 2015; Sodani et al. 2016]. The general idea behind these hybrid systems is to bring the best of two worlds — the bandwidth, latency and energy-efficiency of 3D-stacked DRAM together with the capacity of DIMMs. In these systems, however, good performance requires efficient data allocation and migration between different memory segments. Data management requires profound application profiling, and up to now, no automatic algorithms — whether in the hardware, compiler or runtime environment — can provide out-of-the-box performance for legacy codes. Instead, efficient use of the advanced memory organization is still the responsibility of the programmer, which has significant impact on code development cost [Newburn 2015; Cantalupo et al. 2015; Jeffers et al. 2016].

Therefore, in the context of hybrid memory systems, it is still important to find use cases with (small) memory footprints that fit into the 3D-stacked memory. With good out-of-the-box performance, these use cases would be the first success stories for 3D memory systems. Our study indeed identified the HPC applications and use cases with memory footprints that could be provided by 3D-stacked memory chiplets, making a first step towards adoption of this novel technology in the HPC domain.
2. EXPERIMENTAL SETUP
We analyze the memory footprints of HPC applications running on a large-scale cluster. We first describe our hardware platform and applications, and then we explain how we gather our data.

2.1. Hardware platform
We execute all experiments on the MareNostrum supercomputer [Barcelona Supercomputing Center 2013], one of six Tier-0 HPC systems in the Partnership for Advanced Computing in Europe (PRACE) [PRACE 2016]. MareNostrum contains 3056 compute nodes connected with InfiniBand. Each node contains two Intel Sandy Bridge-EP E5-2670 sockets, each comprising eight 2.6 GHz cores. As in most HPC systems, hyperthreading is disabled. The interconnect is InfiniBand FDR-10 (40 Gb/s), with a non-blocking two-level fat-tree topology offering full bisection bandwidth, built from 36-port leaf switches and 648-port core switches.

The processors connect to main memory through four channels, each with a single DDR3-1600 DIMM. Regular MareNostrum compute nodes include 32 GB of DRAM memory (8 DIMMs \times 4 GB), i.e., 2 GB per core. To study application memory footprints in systems with higher capacity, we execute some experiments on large-memory nodes containing 128 GB of DRAM (8 DIMMs \times 16 GB), i.e., 8 GB per core.

2.2. Applications
We study memory capacity requirements for two widely used HPC benchmarks, High-Performance Linpack (HPL) and High-Performance Conjugate Gradients (HPCG). We also study the Unified European Application Benchmark Suite (UEABS) [PRACE 2013], the set of production applications and datasets designed for benchmarking the European PRACE HPC systems for procurement and comparison purposes [PRACE 2016]. All UEABS applications are parallelized using MPI, and are regularly run on hundreds or thousands of cores. For all applications, we run MPI-only versions, and always execute one MPI process per core. So, in the rest of the paper per-process and per-core memory footprint have equivalent meanings.

2.3. Methodology
In this study, we measure the memory footprints of HPC applications running with various numbers of processes. We obtain footprint information from the \texttt{/proc/[pid]/status} system files, which together log the memory usage of all running processes. The memory footprint of a process corresponds to the amount of physical memory it uses, i.e., the resident set size, or VmRSS. We use the Extrae and Limpio instrumentation tools [Barcelona Supercomputing Center 2014, Pavlovic et al. 2015] to read and log VmRSS values at equidistant time intervals chosen to provide at least 1000 samples per process. We track, in each experiment, the maximums, means, and standard deviations of all memory footprint measurements. For production HPC applications, unless specifically stated that we analyze the master process, we report footprints of worker processes. For HPL and HPCG, we report memory footprints for all the processes.

3. HIGH-PERFORMANCE LINPACK
For more than 20 years, the High-Performance Linpack (HPL) benchmark is the most widely recognized and discussed metric for ranking of HPC systems [Strohmaier et al. 2015]. HPL measures the sustained floating-point rate (GFLOP/s) for solving a dense system of linear equations using double-precision floating-point arithmetic. The linear system is randomly generated, with a user-specified size, so that the user can scale the problem size to achieve the best performance on a given system. The documentation
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Fig. 2. HPL performance also depends on the available memory capacity. When increasing per-core memory, HPL performance first increases and then reaches the saturation point — the sustained floating-point rate (GFLOP/s) of the system. As we increase the number of processes, the saturation point moves towards larger per-core memory capacities.

recommends setting a problem size that uses approximately 80% of the available memory [Petitet et al. 2012]. We determine how reducing the memory capacity would affect performance by appropriately decreasing the problem size. Specifically, we set the problem size in order to use 80% of the target main memory capacity and verify at runtime that the memory footprint fits inside the target memory capacity.

3.1. Measured memory requirements

Figure 2 shows relative HPL performance in FLOP/s (Y-axis) for various amounts of available memory per core (X-axis) and different numbers of processes (different lines on the chart). We plot performance relative to the results with 32 MB of main memory, the smallest amount of memory used in any of these experiments. The experiments are performed for a range of 16–16,384 processes, and in each experiment the number of processes equals the number of cores.

As we increase the available main memory, HPL performance first increases, then reaches the saturation point and remains approximately constant. We observe this trend for any number of HPL processes. Also, we detect that stable HPL performance (after the saturation point) is directly proportional to the number of processes used in the experiment. For instance, increasing the number of processes from 16 to 64, 256, and 1024 increases the steady-state performance by roughly 4×, 16×, and 64× respectively. We also detect that, as we increase the number of processes, the saturation point moves towards larger per-core memory capacities; for instance, 16, 256, and 4096 processes reach their saturation points at 256 MB, 768 MB, and 1280 MB, respectively. This means that for larger HPC clusters, more memory per core is required to achieve maximum HPL performance. When HPL comprises 16,384 processes (executed on one third of the MareNostrum supercomputer), the saturation point reaches 1.5 GB of memory per core. These results indicate that on large HPC systems with tens or hundreds of thousands of high-end x86 cores, reaching the HPL performance saturation point, or at least the point of diminishing returns, requires approximately 2 GB of memory per core. This matches the main memory sizing trends of the large HPC systems that dominate the TOP500 list.

This trend is not visible in Figure 2 because for each number of processes the relative performance is normalized to the 32 MB results.
3.2. Analysis

In order to confirm and better understand our measurements, we analyze how HPL performance depends on single-core floating-point rate, available memory capacity, interconnect bandwidth and latency, and how this dependency changes as we vary the number of processes used in the HPL runs. In this section, we summarize the analysis focusing on the conclusions that have an impact on the memory system sizing; detailed step-by-step explanation and mathematical formulas are presented in the Appendix.

Our analysis confirms the HPL performance trends presented in Figure 2. For small input datasets, HPL has relatively poor overall performances because of high interprocess communication overheads. As the input dataset increases, the computation factor becomes dominant, the communication overhead mitigates and the HPL performance converges to the saturation point. For large per-process memory capacities (large input datasets), the HPL execution time is dominated by the dense matrix-vector multiplication computational routines that require significant processing power. In current HPC systems with gigabytes of main memory, HPL is clearly a CPU bound application typically able to achieve close to the theoretical peak floating-point rate. Our theoretical analysis indeed shows that as the memory capacity is increased, the HPL performance analytically converges to a steady value proportional to the number of processes used in the HPL run, but the performance optimum is theoretically reached for infinite main memory.

We also analytically quantify the HPL performance loss due to a finite main memory capacity and determine the capacity required to reach close-to-optimal HPL performance, e.g., within 10%, 5% and 1% of the optimal. We fit the HPC system parameter constants in the formulas to our experimental data (see Fig. 2) and estimate main memory capacity that will lead to good HPL scores in larger systems. Since we fit the constants to our hardware platform, this analysis shows the trend of the main memory needed to achieve good HPL performance for different system sizes, and not the firm values. The outcome of this analysis is presented in Figure 3.

Figure 3 plots the amount of memory per core (Y-axis) needed to achieve 90%, 95% and 99% of the ideal (infinite memory) HPL performance. We present the results for a wide range of system sizes, from 16 up to over 1,000,000 cores (X-axis). Both axes plot the values in a logarithmic scale. In scaling the interconnect, we assume that latency remains constant and bisection bandwidth scales with the number of cores. This is a conservative assumption because interconnect latency may increase with the number of cores, which would further increase the per-core memory requirement for large systems. From Figure 3, we see that increasing the system size causes more memory per core to be needed to achieve good HPL performance (recall that both axes of Figure 3 have a logarithmic scale). For systems with 100,000 cores, 2.6 GB and 5.5 GB of per-core memory would be needed to reach 90% and 95% of the ideal performance, respectively. This approximately matches the memory sizing of the HPC systems dominating the current TOP500 list. For an HPC system with 1,000,000 cores, however, 7.6 GB and 16.1 GB of per-core memory would be needed to reach 90% and 95% of ideal performance, respectively. To increase efficiency to 99% of the ideal performance, a system with 100,000 cores would require 31.4 GB and a system with 1,000,000 cores would require 88.6 GB per core, a huge amount.

To put our estimation into perspective on Figure 3 we plot three systems: the 16-core system used in the first study that analyzed HPL memory capacity requirements [Don-garra et al. 2003], our largest experiment with 16,384 cores on MareNostrum supercomputer (year 2016), and a future potential 1,000,000-core system. These points val-

---

3In the model developed in the Appendix, $\alpha$ and $\beta$ are constants independent of the number of cores.
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Fig. 3. Per-core memory needed to get 90%, 95% and 99% of the ideal HPL performance, for different sizes of HPC systems. Three systems, with 250 MB/core (year 2003), 2 GB/core (year 2016) and 16.1 GB/core (future potential system) are compared with our estimation curves. Moving from 95% to 99% of ideal HPL performance requires a huge step in the amount of per-core memory (axes are plotted on logarithmic scales).

4. HIGH-PERFORMANCE CONJUGATE GRADIENTS

The High-Performance Conjugate Gradients (HPCG) benchmark [Dongarra et al. 2016] has been introduced as a complement to HPL and the TOP500 rankings, since the community questions whether HPL is a good proxy for production applications. HPCG is based on an iterative sparse-matrix conjugate gradient kernel with double-precision floating-point values, and is representative of HPC applications governed by differential equations. Such applications tend to have much greater demands on the memory system, in terms of bandwidth and latency, and they access data using irregular patterns [Dongarra and Heroux 2013]. Similarly to HPL, the user can scale the problem size to achieve the best performance on a given system. Therefore, to determine the capacity requirements, we analyze HPCG performance for a range of 16–8192 processes as a function of the problem size, i.e., main memory used in the experiment. Then, we analyze whether the trends detected in the real-system measurements match the expected tendencies based on algorithm complexity and data pattern accesses.

4.1. Measured memory requirements

In Figure 4, we show the relation between relative HPCG performance (Y-axis) and memory footprint (X-axis). We executed HPCG for various memory footprints, by changing the problem sizes from 24-24-24 up to 120-120-120 with an additive step of 8, always keeping the three dimensions identical, and reported average per-process memory footprints. For each number of processes, the performance was plotted relative to the results with the smallest problem size used in the experiments. We analyzed this trend for different numbers of processes that are plotted with different lines of the chart. Recall that, for each experiment, the number of processes equals the number of cores.

For a small number of processes and small input datasets, the HPCG workload may (partially) fit into on-CPU caches which leads to performance that significantly exceeds stable ones (on larger input datasets). In our experiments, we detected this trend for 16 and 32 processes. This trend is detected and analyzed by previous studies [Marjanović et al. 2014], and it is considered to be a non-representative use of HPCG [Dongarra et al. 2014; 2016]. Therefore, we neither plot nor analyze these results.
Fig. 4. HPCG performance also depends on the available memory capacity. Performance increases until it reaches the saturation point, where it is constrained by the sustained memory bandwidth. The saturation point remains constant across a wide range of HPCG processes, at around 512 MB of main memory per process.

As we increase the HPCG problem size, i.e., per-process memory footprint, HPCG performance rapidly increases and then reaches a stable value directly proportional to the number of processes used in the experiment.\footnote{As for HPL, this trend is not visible in Figure 4 because for each number of processes, the performance is normalized to the result with the smallest input dataset.} Unlike HPL, we detect that the saturation point remains constant, roughly 512 MB of main memory per-process, for a large range of HPCG processes. In the following section, we analyze this in detail. Finally, we also detect that for memory footprints of around 1.5 GB, HPCG performance decreases. The performance drop is caused by swapping, and we did not detect it when the experiments were repeated on large-memory nodes comprising 8 GB of main memory per core. The HPCG performance drop because of memory swapping was not reported in past, and we would suggest that HPCG developers take this into account when providing suggestions about dataset sizing.

4.2. Analysis

Although the HPCG benchmark was released only a couple of years ago, several studies analyze its behavior and performance bottlenecks, and even estimate its performance on future exascale HPC systems [Marjanović et al. 2014; Park et al. 2014]. When running HPCG, the user sets the per-process problem size \(N\). For a given problem size \(N\), the number of floating-point operations and memory accesses are both proportional to \(N\).

\[
#FLOPs_{\text{per\ process}} \approx O(N)
\]  

The execution time of HPCG depends on the problem size \(N\) and number of processes \(n\):

\[
T \approx O(N) + O(N^{\frac{2}{3}}) + O(\log n)
\]  

The first factor \(O(N)\) refers to the computational complexity, while factors \(O(N^{\frac{2}{3}})\) and \(O(\log n)\) refer to point-to-point and collective communication, respectively.

For small memory capacities, below 256 MB per process in Figure 4, the HPCG performance is affected by the interprocess communication, factors \(O(N^{\frac{2}{3}})\) and \(O(\log n)\) in Equation 2. However, as the input dataset increases, the factor \(O(N)\) becomes dominant and the communication overhead mitigates; the HPCG performance rapidly converges to the saturation point determined by the memory bandwidth.

For large per-process memory capacities (large values of \(N\)), the HPCG execution time is dominated by the computational routines, which mainly perform sparse matrix-vector multiplication [Dongarra and Heroux 2013] and require modest CPU power but...
The memory footprints of an HPC application executed with a given input dataset can vary significantly for different numbers of application processes. In general, the more processes used for the computation, the smaller the portion of the input data handled.
Table I. Scientific HPC applications used in the study

<table>
<thead>
<tr>
<th>Application</th>
<th>Area of science</th>
<th>Test Case A: Smaller input dataset</th>
<th>Test Case B: Larger input dataset</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Problem size</td>
<td>Process range</td>
</tr>
<tr>
<td>ALYA</td>
<td>Computational mechanics</td>
<td>27 million element mesh</td>
<td>16–1k</td>
</tr>
<tr>
<td>BQCD\a</td>
<td>Particle physics</td>
<td>32\times64\times lattice</td>
<td>64–8k</td>
</tr>
<tr>
<td>CP2K</td>
<td>Computational chemistry</td>
<td>Energy calculation of 1024 waters</td>
<td>128–1k</td>
</tr>
<tr>
<td>GADGET</td>
<td>Astronomy and cosmology</td>
<td>135 million particles</td>
<td>512–8k</td>
</tr>
<tr>
<td>GENE</td>
<td>Plasma physics</td>
<td>Ion-scale turbulence in Asdex-Upgrade</td>
<td>64–1k</td>
</tr>
<tr>
<td>GROMACS</td>
<td>Computational chemistry</td>
<td>150,000 atoms</td>
<td>16–1k</td>
</tr>
<tr>
<td>NAMD</td>
<td>Computational chemistry</td>
<td>2\times2\times2 replication of the STM Virus</td>
<td>16–1k</td>
</tr>
<tr>
<td>NEMO</td>
<td>Ocean modeling</td>
<td>12\times global configuration; 4322\times3059 grid</td>
<td>512–8k</td>
</tr>
<tr>
<td>QE</td>
<td>Computational chemistry</td>
<td>112 atoms; 21 iterations</td>
<td>16–1k</td>
</tr>
<tr>
<td>SPECFEM3D</td>
<td>Computational geophysics</td>
<td>6\times12\times768 mesh of the earth</td>
<td>864</td>
</tr>
</tbody>
</table>

\a Quantum Chromo-Dynamics (QCD) is a set of five kernels. We study Kernel A, also called Berlin Quantum Chromo-Dynamics (BQCD), which is commonly used in QCD simulations.

\b CP2K cannot run Test Case B on our platform. The errors have been reported to the application developers.

by each process. On the other hand, distributing the computation over a larger number of processes also means more replication of data on the boundaries of adjacent data segments, or in per-process private data segments, external libraries, and communication buffers [Koop et al. 2007]. Although it may seem obvious that memory footprints of HPC applications are tightly-coupled with the number of application processes, previous studies of memory footprints ignore this relationship (see Section 7).

Figure 5(a) illustrates the relationship between the per-process (per-core) memory footprint and the number of application processes for NAMD running Test Case A. This is a strong scaling case, i.e, we keep the same input dataset (Test Case A) and change the number of processes. This corresponds to a real-life use of production applications in which users have to choose the number of processes that will be used to solve an already defined problem with a fixed input size. For each process we track the maximum and mean memory footprints, and we plot the average values and the standard deviations among all processes. When NAMD runs as 16 processes, the mean per-process memory footprint is 1656 MB. As we increase the number of processes, the footprint drops significantly. When the application runs using 1024 processes, the per-process memory footprint is only 258 MB, a difference of 6.4\times. Maximum memory footprints exhibit the same trends (see Figure 5(a)), and thus in the rest of the paper we discuss only mean footprint values.

Figure 5(b) summarizes memory footprint results for all UEABS workloads. Except GROMACS, which has a small overall memory footprint, the general trend is the
same for the remaining applications. We detect memory footprint changes from $3.3 \times$ for CP2K up to $17 \times$ for ALYA.

5.1.1. Discussion. Our analysis emphasizes that the memory footprints of HPC applications are tightly-coupled with the number of application processes. State-of-the-art parallel benchmark suites, however, do not strictly define the number of processes to use in experiments. UEABS recommends experiments with up to 10,000 processes, but the minimum number of processes is not specified. Similarly, other parallel benchmark suites either provide loose recommendations about the number of processes (SPEC OMP2012 [SPEC 2015b], SPEC MPI2007 [SPEC 2015a], SPLASH-2 [Woo et al. 1995]) or do not discuss this issue at all (NAS [Wong et al. 1999], PARSEC [Bienia et al. 2008], HPC Challenge [Luszczek and Dongarra 2005], Berkeley dwarfs [Asanovic et al. 2006]). Therefore, when analyzing memory capacity requirements, it is essential that the users themselves determine a number of processes that is representative of real production use. This, in turn, requires knowledge of the HPC category that the user is targeting together an understanding of the scalability of the applications under study, as we discuss in the following sections.

5.2. Selecting the number of processes

5.2.1. HPC categories. High-performance computing is broadly divided into two categories [ETP4HPC 2013]. Capability computing refers to using a large-scale HPC installation to solve a single problem in the shortest possible time, for example simulating a human brain on a Tier-0 HPC system. Capacity computing refers to optimizing system efficiency to solve as many mid-size or smaller problems as possible at the same time at the lowest possible cost, for example when small or medium enterprises use rented (on-demand) HPC resources to simulate numerous design choices for their products. Analyzing pricing policies for renting HPC resources is beyond the scope of this study; in the rest of this paper, we therefore approximate the cost of a given experiment as proportional to the CPU-hours, i.e., the number of cores used in the experiment ($\#\text{cores}$) multiplied by the execution time: $\text{cost} \propto \text{CPU hours} = \#\text{cores} \times \text{exe.time}$.

Although capability computing targets application runs with the lowest execution time, excessive application scaling may deliver diminishing returns in performance improvement while linearly increasing CPU-hours. This is an unacceptable scenario that leads to inefficient resource utilization. Similarly, although capacity computing targets low-cost HPC computation, excessive slowdown of application runs may have unacceptable impact, e.g., on the productivity of engineers waiting for simulation results.

5.2.2. Application scalability. It is important to understand that CPU-hours and execution time are dependent metrics, and that in the production runs, users must analyze the trade-offs between them. In Figure 6, we analyze this relationship for NAMD
and CP2K, respectively. The upper graphs of Figures 6(a) and 6(b) show normalized speed-up and CPU-hours for each experiment, and the lower graphs show application parallel efficiency. All statistics are computed relative to the experiments with the fewest processes, 16 for NAMD and 128 for CP2K. Parallel efficiency (a number between 0 and 1) quantifies how effectively the resources are utilized, and it is the main metric for analyzing application scalability. A parallel efficiency of 1 means that the application speed-up is directly proportional to the number of processes. Low parallel efficiency means that significantly increasing processing resources only delivers low or moderate speed-ups.

NAMD is an example of an application with good scalability (Figure 6(a)). Increasing the number of processes causes significant speed-ups with negligible increments in CPU-hours. When we change the number of processes from 16 to 256, 512, and 1024, we measure speed-ups of $14.60 \times$, $27.79 \times$, and $39.14 \times$ at cost increments of 10%, 15%, and 64%, respectively. When used in capability computing, NAMD should be executed with a large number of processes (we use 1024 processes in the experiments presented in Figure 6(a)). Although CPU-hours is the primary metric in capacity computing, it is reasonable to expect that a user would accept small increases in CPU-hours if they lead to high (e.g. 42-fold) improvements in execution time. Therefore, in capacity computing as well, experiments with a large number of processes are most representative of real-life production use of NAMD. We observe similar trends for ALYA, BQCD, GENE, and Quantum Espresso. All of them show good scalability and significant speed-ups with negligible CPU-hours increments. In both capability and capacity computing, these applications should be executed with many processes.

CP2K is an example of an application with limited scalability (Figure 6(b)). When we change the number of processes from 128 to 256, 512, and 1024, we observe speed-ups of $1.77 \times$, $2.71 \times$, and $3.98 \times$, while the CPU-hours increase $1.13 \times$, $1.48 \times$, and $2.01 \times$, respectively. Results for CP2K show clear trade-offs between cost and speed-up. When used in capability computing, CP2K should be executed with a large number of processes, 512 and 1024 in the experiments presented in Figure 6(b). When targeting capacity computing, users should try to reduce CPU-hours. Thus, CP2K should be par-

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Fig. 6. Trade-offs between normalized execution time and experiment cost (CPU-hours) for applications with good and limited scalability.

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Recall that CP2K cannot be executed with 16, 32 and 64 processes because its memory requirements exceed the available memory.
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Large number of processes

Large number of processes

Large number of processes

Small number of processes

HPC category

Large
number of processes

Small
number of processes

Application scalability

Good

Limited

Capability

computing

Capacity

computing

Fig. 7. The representative number of application processes is determined by application scalability and the targeted HPC category.

We observe similar behavior for GADGET, GROMACS, and NEMO.

5.2.3. Summary. In this section, we showed how memory footprints of HPC applications depend on the number of application processes, and we provided guidelines for selecting the number of processes to be representative of production application use. Figure 7 summarizes this analysis. The figure shows how the representative number of application processes depends on application scalability and how this may change for different HPC categories. Applications with good scalability should be executed with large numbers of processes, regardless of the targeted HPC category. This leads to significant speed-ups with only a small increase in experimentation cost. For applications with limited scalability, increasing the number of processes reveals a clear trade-off between execution time and CPU-hours. For experiments that target capability computing, these applications should be executed with a large number of processes providing low execution time at the expense of the CPU-hours. On the other hand, when targeting capacity computing, applications should be partitioned into a small number of processes, sacrificing execution time to improve experimentation cost and overall system throughput [Zivanovic et al. 2016].

5.3. Memory requirements of production HPC applications

In this section, we analyze per-process memory capacity requirements of the production applications. In all experiments, the applications were run with Test Case A inputs and up to 8192 processes. Test Case A can be run for all UEABS applications, and it supports a wider range of processes compared to Test Case B (which could only run six out of ten applications, see Section 2.2). We analyze Test Case B in more detail in Section 5.4. Recall that our applications roughly scale up to 1000–10,000 processes when running these input datasets.

The results are summarized in Figure 8. The left side of Figure 8 shows results for the applications with good scalability — ALYA, BQCD, GENE, NAMD, and Quantum Espresso (QE). These applications should be executed with a large number of processes regardless of the targeted HPC category. The average per-process memory footprints for these applications ranges from 57 MB for ALYA to 258 MB for NAMD. The footprints for BQCD, GENE, and QE are 116 MB, 137 MB, and 197 MB, respectively.9

9Although Quantum Espresso processing Test Case A should scale up to 1024 processes [PRACE 2013], we observed very good scalability up to 256 processes but poor scalability (slowdowns) for 512 and 1024 processes. We therefore report results for 256 processes for this application.
The right side of Figure 8 shows the per-process memory footprints of the applications with limited scalability. In the capability computing experiments, we execute these applications on a large number of cores: 1024 for CP2K, and 8192 for GADGET and NEMO. The per-process memory footprints are again fairly small — 336 MB, 154 MB, and 203 MB, for CP2K, GADGET, and NEMO, respectively. Since the processor under study has eight cores, and we allocate one process per core, the per-socket memory footprint in these experiments ranges between 0.4 GB (ALYA, 8 × 57 MB) and 2.6 GB (CP2K, 8 × 336 MB). The first-generation 3D memory devices already provide such memory capacities, see Section 6.1.

In capacity computing, we execute the applications with limited scalability on a small number of cores, and this number is dictated by the memory capacity of the compute nodes — scaling the parallelism down further would cause the per-process memory footprints to exceed the available memory. To understand how the memory footprints increase in systems with higher memory capacities, we run experiments on large-memory nodes containing 128 GB of main memory, i.e., 8 GB per core. When we partition CP2K, GADGET, and NEMO to 16, 256, and 128 processes, their per-process footprints are 5.8 GB, 2.2 GB, and 4.8 GB, respectively (rightmost part of Figure 8). On standard nodes with 2 GB of memory per core, we could partition these applications to 128 processes for CP2K, and 512 processes for GADGET and NEMO. In this scenario, we measured the per-process memory footprints of 1.1 GB, 1.2 GB, and 1.3 GB, for CP2K, GADGET, and NEMO, respectively.

Figure 8 omits results for GROMACS and SPECFEM3D. The per-process footprint of GROMACS is very low, between 60 MB and 70 MB, and it decreases only slightly from 16 to 1024 processes (see Section 5.1). SPECFEM3D requires exactly 864 processes, and thus we cannot analyze how its memory footprint changes with the number of processes. When executed with 864 processes, the average memory footprint is 2.53 GB.

These results show that different production HPC applications — or even a single application used in different HPC categories — can have significantly different memory capacity requirements. Applications that scale well and those that target capability computing have low per-process memory footprints. These applications require from 57 MB to 258 MB of memory, which means that they heavily under-utilize the memory capacity of our HPC platform: their average memory usage is below 10% of the full capacity. Only the applications with limited scalability that target capacity computing require gigabytes of main memory per process.

5.3.1. Master process memory requirements. Many HPC applications are written using a master–worker process model. In these applications, the problem is decomposed into
As the number of processes increase, memory footprints of worker processes decrease as expected, but memory footprint of the master process increases: ALYA, Test Case A.

Figure 9 plots the memory footprints of the ALYA master and worker processes as the number of processes increases from 16 to 1024. Memory footprints of worker processes drop as we increase the number of processes, following the trend described in Section 5.1. The master process, however, exhibits the opposite trend, and its memory footprint increases with the number of processes. This is a general trend in master–worker applications. For the UEABS applications, we detect that master process may have significantly higher memory footprints than workers, up to $36.6 \times$ for NEMO (master 7.2 GB, worker 0.2 GB) and $62.5 \times$ for BQCD (master 7.1 GB, worker 0.1 GB). Both application developers and computer architects should pay attention to this phenomenon, still not well highlighted and quantified by the community.

5.4. Towards weak scaling analysis

The presented analysis keeps constant the input dataset size and varies the number of application processes. This refers to the strong scaling case of production HPC applications. In addition to this, it is also important to perform a weak scaling analysis, i.e., to analyze memory capacity requirements when both the number of processes and input dataset size are increased — similar to the study performed for HPL and HPCG benchmarks. Since the problem inputs are specified by the benchmark suite, such analysis requires either that the benchmark suite support a user-defined problem size (as for HPL and HPCG) or that it provides a set of inputs specifically intended for weak scaling analysis. We are not aware of such a real application benchmark suite. UEABS for instance has just two problem sizes, Test Case A and Test Case B, and in many cases the problems being solved are fundamentally different, making them unsuitable for weak scaling analysis. For example, in case of ALYA, Test Case A is a model of the respiratory system whereas Test Case B is a mesh of generic elements [Bull 2013]. As an intermediate step, we analyze the two input datasets for the NAMD benchmark distributed with the UEABS suite, which is one of few benchmarks where the two datasets are comparable [Bull 2013], and observe the changes in the application memory footprint and scalability when increasing the input dataset size.

In order to analyze how the per-process memory footprint changes with dataset size, in Figure 10(a) we plot the NAMD memory footprint results for both the smaller and larger input datasets. The Test Case A curve starts at 16 processes, a single MareNostrum node. Test Case B exceeds the memory capacity of one or two MareNostrum nodes (16 and 32 processes), so the curve starts from 64 processes. We show the Test Case A results on up to 1024 processes, and for Test Case B on up to 8192 processes, as recommended by UEABS documentation [PRACE 2013]. For both input
datasets, the NAMD footprint is around 1600 MB on a small number of processes, and it drops rapidly as we increase the process count. Both memory footprint curves follow the same tendency, with the Test Case B results being shifted towards larger numbers of processes. We detect the same trend for all UEABS applications.

Next, we analyze the impact of dataset size on application scalability. Figure 10(b) plots parallel efficiency of NAMD with both input datasets. Parallel efficiency of NAMD with Test Case A reduces to 0.61 when the process count increases from 16 to 1024 ($64 \times$). With Test Case B, when increasing from 64 to 2048 processes ($32 \times$), the parallel efficiency drops to 0.39.\textsuperscript{10} For all the applications under study, we find that it is harder to achieve good scalability for larger numbers of processes, even if the input dataset size increases. This is not surprising, because increasing the number of processes causes more communication and synchronization overheads, and increases the penalty of sequential code segments. The simple increase in dataset size does not address all of these problems.

To summarize, our results show that when input datasets increase, the memory footprint as a function of the number of processes keeps the same trend, but the curve is shifted toward larger number of processes (Figure 10(a)). Application scalability, however, reduces, in some cases significantly. Therefore, increasing the input dataset requires repeating the analysis of the trade-offs between execution time and CPU-hours (Section 5.2) in order to determine the representative number of processes for a production run of the application.

6. IMPLICATIONS

The current trend in HPC system design is to increase the number of memory channels per CPU and the number of I/Os in each DDR generation. This approach is limited by the package size, plus it is expensive, and it increases memory system power consumption. A potentially promising solution for these problems is the use of 3D-stacked DRAMs. In this section, we summarize the pros and the cons of 3D-stacked DRAM, and briefly overview the currently-available products based on this technology: Hybrid Memory Cube (HMC), High-Bandwidth Memory (HBM), and multi-channel DRAM (MCDRAM) incorporated into the Knights Landing processors. We also discuss the opportunities and challenges of these solutions in the context of high-performance computing, and outline our expectations on how these devices may change the design of next-generation memory systems.

\textsuperscript{10}NAMD running Test Case B should scale up to 10,000 processes, but we detect very low or no speed-up after 2048 processes. Therefore we plot parallel efficiency results up to 2048 processes for Test Case B.
6.1. Background: 3D-stacked DRAM

3D stacking increases package density, with memory chiplets placed on a silicon interposer instead of a printed circuit board. Stacked DRAM dies are connected using through-silicon vias (TSVs), which shorten the interconnection paths and reduce connectivity impedance and channel latency. Hence, data can be moved at a higher rate with a lower energy per bit. On the down side, 3D-stacked DRAMs will likely reduce the main memory capacity, at least in early generations, due to significantly higher cost per bit than conventional DIMMs.

**Hybrid Memory Cube (HMC)** [HMC Consortium 2014] is connected to the CPU with a high-speed serial interface that provides up to 480 GB/s per device. Announced production runs of HMC components are limited to 2 GB and 4 GB devices, while the standards specify capacities of up to 8 GB. Memory capacity can be increased by integrating multiple HMC devices into the package, but doing so is non-trivial. Each HMC device can be directly connected to up to four other devices (CPUs or HMCs) via four independent serial links. This enables chaining of devices to increase memory capacity, but multi-hop routing may increase access latency and variability. The impact of such variability on HPC workloads requires further analysis and justification.

**High-Bandwidth Memory (HBM)** [JEDEC 2013] is connected to the host CPU or GPU with a wide 1024-bit parallel interface that delivers up to 256 GB/s. Similarly to HMC, the standard specifies up to 8 GB devices and integrating multiple devices in the package is challenging. Only a single HBM device can be connected to each interface (channel), so using multiple HBM devices requires a large silicon interposer with multiple 1024-bit wide interfaces, increasing cost.

**Intel Knights Landing (KNL)** processors [Sodani et al. 2016] are the first CPUs that bring in 3D-stacked DRAM in addition to the traditional DDR DIMMs. KNLs comprise up to 72 cores supported by two levels of main memory. At the first level, **3D multi-channel DRAM (MCDRAM)** is connected to the CPU through an on-package interposer and it offers a capacity of up to 16 GB (0.2 GB per core) with 400 GB/s of peak theoretical bandwidth. In addition to MCDRAM, KNL can be connected to up to 384 GB (5.4 GB per core) of standard DDR4 memory. MCDRAM and DDR can be organized in three modes: cache, flat and hybrid. In the cache mode, MCDRAM behaves as an additional (L3) level of the cache hierarchy. In the flat mode, MCDRAM and DDR are two distinct memory nodes with different capacity, latency and bandwidth that can be addressed by different APIs. In case that the input dataset does not fit into the MCDRAM, it is responsibility of the programmer to perform data partitioning, allocation and migration that would use efficiently the advanced memory organization. Finally, the hybrid mode combines the cache and the flat mode. In this mode, the MCDRAM is partitioned into two segments — one is used as the L3 cache for the DDR, while the other is addressable and used as MCDRAM memory node in the flat mode.

6.2. 3D-stacked DRAM in HPC memory systems: Opportunities and challenges

Understanding application memory capacity requirements is essential for the design of HPC memory systems based on 3D-stacked DRAM. The main question to be answered is whether 3D memory chiplets can on their own provide the capacity required by HPC applications.

6.2.1. HPCG vs. HPL. An important driving force for 3D-stacked DRAM could be the HPCG benchmark. With performance directly proportional to main memory bandwidth, and memory footprints below 1 GB per process even when targeting million-core systems, HPCG could be the first success story for 3D-stacked DRAM in HPC. Regarding KNL, hundreds of MBs per core of MCDRAM may be sufficient for an outstanding HPCG performance, especially on small clusters (see Figure 4). Therefore,
HPCG could be a good example of an important benchmark that works out-of-the-box and performs well on KNL.

On the other hand, one of the main show-stoppers for 3D-stacked memory could be HPL. In contrast to HPCG, high memory bandwidth provides no benefits for HPL, while the limited capacity of 3D-stacked memory can lead to significant performance loss, especially in large-scale systems. As shown in Section 3.2, a million-core system would require 16.1 GB per core to achieve 95% of the potential performance (Figure 3). Although the HPC community is questioning whether HPL is representative of modern production HPC applications [Murphy et al. 2006; 2010], and is actively looking for alternative benchmarks (HPCG being one of them), high HPL scores are still important objectives in the design of large HPC clusters. Looking forward, it will be interesting to see whether KNL-based TOP500 systems will use the 3D-stacked MCDRAM in the HPL runs, i.e. whether the developers of optimized HPL and corresponding linear algebra libraries will find a way to benefit from hybrid MCDRAM + DDR memory systems.

6.2.2. Production HPC applications. In Section 5.3 and Figure 8 we saw that the memory capacity requirements of production HPC applications had a bimodal distribution. Most of our HPC applications and use cases require only hundreds of megabytes of main memory. This capacity can be provided by 3D memory chiplets located on the silicon interposer (e.g. KNL MCDRAM), with no need for conventional DIMMs on the printed circuit board (PCB). Such a memory will provide significantly higher memory bandwidth and lower latency, which, in turn, will lead to higher system performance and energy-efficiency. Since 3D-stacked memory chiplets could directly replace DIMMs, the main memory would still comprise a single level with uniform latency.

For HPC applications that require gigabytes of main memory, sufficient memory capacity can be provided using hybrid 3D memories plus on-PCB DIMMs, similar to KNL systems. The main memory would therefore consist of two levels of hierarchy with different latencies, bandwidths, and capacities. For computer architects, this opens design options to optimize the capacities, organizations, and interconnections of the 3D memory chiplets and the DIMMs.

Although hybrid memory systems support functional portability, i.e. execution of legacy codes, there is a clear tradeoff between the achieved performance and the effort invested in code profiling and development. For example, in the KNL cache mode, large-footprint applications can be executed with no changes in the source code, but this approach could lead to significant performance loss. Although having large caches may intuitively suggest higher performance, in KNL it may not be the case. Since MCDRAM and DDR4 have separate data paths (as they use separate memory controllers), MCDRAM misses require two consecutive accesses — first to the MCDRAM and second to the DDR — leading to a high cache miss penalty and potentially low overall performance.

Good performance of hybrid memory systems is conditioned by the need for advanced data allocation, migration, and prefetching policies [Chou et al. 2014; Meswani et al. 2015]. Optimal data management in these systems, such as the KNL flat memory mode, requires profound application profiling and a significant increase in the code development cost. In order to reduce this effort and increase adoption of the KNL architecture, Intel released various profiling tools [Intel 2016a] and data management libraries and APIs [Intel 2016b] that simplify efficient programing of the systems with hybrid main memory. It will be interesting to see whether the KNL — as the first system that combines the 3D-stacked and the DDR main memory — will be adopted by the users, and whether the increased cost in software development and maintenance will be justified by the performance gains.
6.2.3. Message from application developers. New HPC systems should be designed taking into consideration the requirements from future users and application developers. With regard to memory capacity, certain applications, in domains such as theoretical physics and inorganic chemistry, have a constant need for more memory. Based on Figure 8, however, we see that there are many applications that have low memory requirements. Users of such applications that could in fact live with less DRAM usually remain quiet, since for them the additional DRAM under discussion will not degrade performance. Moreover, these users generally do not have to pay the costs associated with extra memory per core, in terms of capital cost and power consumption. This leads to general-purpose HPC clusters with 2 GB per high-end x86 core, with some large-memory nodes having 4 GB to 8 GB per core, i.e., more than 100 GB per node.

With the introduction of 3D-stacked memory, this dynamic changes. Users may wish to “trade” DIMM capacity, which they do not need, for 3D-stacked DRAM, which provides higher bandwidth and lower latency. For applications with relatively low memory capacity requirements, 3D-stacked DRAM is likely to lead to significantly better overall performance [Radulovic et al. 2015]. It is therefore essential that application developers understand the performance–capacity–cost tradeoffs between DIMM-based, 3D-stacked and hybrid DRAM solutions, in order to clearly express their preferences to the HPC hosting centres. Whereas user demand has already led to large-memory nodes, messages from the users and developers of small-memory application may lead to specialization in the other direction; i.e., small-memory nodes with high-bandwidth low-latency 3D-stacked memory.

7. RELATED WORK
Dongarra et al. [2003] present the Linpack benchmarks suite, the TOP500 list, and the HPL code. The authors execute HPL on a small 4×4 cluster of Pentium III 500 MHz CPUs and analyze the benchmark performance for various interconnects and input dataset sizes of up to around 250 MB per core. The results show that increasing the HPL input dataset size can lead to significant performance improvements. Our work extends this study in various directions. We detect the point of diminishing returns when increasing the input dataset size, and analyze how this changes with the number of processes used in the HPL run, i.e., with the size of the HPC system. We also estimate the amounts of physical memory required for the close-to-optimal HPL performance on future large-scale HPC clusters.

The HPL benchmark has been extensively used in the past. In general, HPL studies analyze how to tune arithmetic libraries, OS kernel and network parameters to improve HPL performance on a given system. The studies use the maximum input dataset that fits into the physical memory while preventing swapping, as suggested by the HPL developers, and do not analyze the impact of changes in the physical memory capacity on the HPL performance.

Marjanović et al. [2014] analyze the HPCG benchmark and predict the HPCG performance on a given architecture based on the memory bandwidth and the highest network latency between compute units. They conclude that for modern systems with a decent network, highly accurate prediction can be done based only on the memory bandwidth. On the node level, they show that small problem sizes that fit in the CPU caches can have HPCG performance that exceeds the stable values and are therefore non representative. However, they do not analyze how HPCG performance depends on the problem size for larger numbers of processes, as we did in this study.

Although memory provisioning for large-scale HPC clusters is an important task, to the best of our knowledge only three prior studies analyze memory footprints of HPC applications [Biswas et al. 2011; Perks et al. 2011; Pavlovic et al. 2011]. However, these studies do not analyze the relationship to the number of processes, which is very impor-
tant as we show in this study. Biswas et al. [2011] and Perks et al. [2011] investigate different techniques to reduce memory footprints in order to improve the performance of HPC workloads. Biswas et al. [2011] leverage the data similarity often exhibited in MPI applications. They identify identical memory blocks across MPI tasks on a single node and use a novel memory allocation library to merge them. The authors evaluate their proposal on a range of MPI applications (SPEC MPI2007, NAS, ASC Sequoia benchmarks, and two production applications), and show memory footprint reduction of 32% on average. Perks et al. [2011] investigate the impact of compiler choice on the memory usage of distributed MPI codes. The authors compare memory usage of four versions of simple MPI benchmarks compiled with GNU, Intel, PGI, and Sun compilers. Their results show that compiler choice can make a difference of up to 32% in memory usage. Pavlovic et al. [2011] characterize memory behavior for four scientific applications to estimate the memory system requirements of future HPC systems with hundreds or thousands of cores per node. The authors estimate memory footprints of HPC applications comprising thousands of processes by using linear regression based on results of a few experiments with a small number of processes. Even though the authors target systems running applications with thousands of processes, the study does not analyze application scalability, nor does it evaluate whether the input sets used in the study are large enough to take advantage of such parallelism.

As the first 3D-stacked DRAM devices are hitting the market, various studies analyze how to incorporate these devices into the memory hierarchy. It is generally accepted that 3D-stacked DRAM is unlikely to fulfill the memory capacity requirements of server and HPC applications, so the community is exploring hybrid systems in which 3D-stacked DRAM is complemented by standard DIMMs [Dong et al. 2010; Chou et al. 2014; Sim et al. 2014; Meswani et al. 2015]. The essence of these studies is the development of techniques for advanced data migration between 3D-stacked DRAM and DIMMs. An important requirement of this work is to avoid excessive code development costs and improve performance of legacy codes. So, all the studies keep the unified view of the main memory at the application level; the data management policies are performed in hardware by complex data path enhancements [Chou et al. 2014; Sim et al. 2014] or by an interaction between hardware and the operating system [Dong et al. 2010; Meswani et al. 2015]. Overall, all studies agree that managing hybrid memory systems with 3D and DIMMs is a difficult task and that simple approaches, such as using 3D-memory as an additional level of cache, may lead to significant performance loss.

8. FUTURE WORK

A simple but important question “How much memory do we need in HPC?” has not been discussed thoroughly by the academic and computer architecture community. We hope that our study will trigger further research and discussion on this topic. The first topic for future work could be an analysis of weak scaling of production HPC applications and its impact on HPC memory footprints. Weak scaling analysis is especially important to anticipate future HPC problems with significantly larger input datasets. This analysis, however, would require HPC production application benchmark suites that allow the problem size to be tuned in a similar way to HPL and HPCG, or at least provide a collection of comparable input sets with varying problem size.

Also, the community, or at least large research centers that purchase HPC clusters should question the current trends for memory system sizing. Maybe the first steps could be to study the histograms of memory system usage of existing HPC clusters and understand whether users are taking advantage of most of the installed memory. It seems that decisions for new machines have traditionally been based on experiences with previous HPC clusters and on undocumented knowledge of the principal system
integrators. This is a conservative approach that will unlikely lead to a breakthrough in the memory system design.

Finally, the principal HPC system designers and integrators should publicly document and justify their memory sizing decisions. For example, based on our results, one could question whether the memory capacity of the largest HPC clusters are provisioned with too much emphasis on the TOP500 list. Since smaller HPC systems are influenced by the system architectures of the larger ones, this could mean that the HPL scores are responsible for most of the HPC memory system sizing decisions. It is about time that HPC system designers try to convince us that this is not true, and explain the real rationale behind the 2–3 GB per-core rule.

9. CONCLUSIONS
This study analyzed memory capacity requirements of important HPC benchmarks and applications. This analysis becomes increasingly important as 3D-stacked memories are hitting the market. These novel memories provide significantly higher memory bandwidth and lower latency, leading to higher performance and better energy-efficiency. However, the adoption of 3D memories in the HPC domain requires use cases needing much less memory capacity than currently provisioned. With good out-of-the-box performance, these use cases would be the first success stories for these memory systems, and could be an important driving force for their further adoption.

We detected that HPCG could be an important success story for 3D-stacked memories in HPC. With low memory footprints and performance directly proportional to the available memory bandwidth this benchmark is a perfect fit for memory systems based on 3D chiplets. HPL, however, could be one of the main show-stoppers because reaching a good performance requires memory capacities that are unlikely to be provided by 3D chiplets.

The study also emphasizes that the analysis of memory footprints of production HPC applications requires an understanding of their scalability and target category, i.e., whether the workloads represent capability or capacity computing. The results show that most of the HPC applications under study have per-core memory footprints in the range of hundreds of megabytes — an order of magnitude less than the main memory available in the state-of-the-art HPC systems; but we also detect applications and use cases that still require gigabytes of main memory.

Overall, the study indeed identified the HPC applications and use cases with memory footprints that could be provided by 3D-stacked memory chiplets, making the first step towards adoption of this novel technology in the HPC domain. Also, it showed that the simple question “How much memory do we need in HPC?” may not have a simple answer. We hope that this will motivate the community to question the trends for memory system sizing in current HPC clusters, and will lead to further analysis targeting future ones.

APPENDIX: HPL ANALYTICAL ANALYSIS
The Appendix complements the HPL analysis in Section 3.2; it presents step-by-step mathematical formulas that analyze HPL performance as a function of per-core memory capacity and the number of processes. The analysis indeed shows that the HPL performance analytically converges to a steady value proportional to the floating-point rate (GFLOP/s) of the system, but the performance optimum is theoretically reached for infinite main memory. We also calculate the per-core memory capacity needed to achieve steady values of HPL performance, and how this amount of memory changes when increasing the size of HPC systems (number of cores).

Number of FLOPs. HPL solves a dense linear system of $N$ unknowns using LU factorization [Petitet et al. 2012]. For a given problem size $N$ the benchmark performs
the following number of double-precision floating-point operations (#FLOPs) [Dongarra et al. 2003]:
\[
#\text{FLOPs} = \frac{2}{3} N^3 + 2N^2 + O(N) \tag{3}
\]
Since \( N \gg 1 \), and for number of processes \( n \):
\[
#\text{FLOPs} \text{per process} \simeq \frac{2}{3} n \tag{4}
\]

**Execution time.** HPL execution time on a specific system depends on various system parameters:

- \( \gamma_3 \): The time that a single processing unit (e.g. CPU core) requires to perform one floating-point operation when performing matrix-matrix operations.
- \( \alpha \): The time to prepare a message for transmission between processes.
- \( \beta \): The time \( L \times \beta \) indicates the time taken by the message of length \( L \) to traverse the network to the destination.

The execution time also depends on the way the data (matrices) are partitioned and distributed among the processes. The coefficient matrix is first logically partitioned into blocks, each of dimension \( N_B \times N_B \), and these blocks are cyclically distributed onto the process grid. In all our experiments, factor \( N_B \) is kept constant. Finally, the data is distributed onto a two-dimensional grid of processes, \( P \times Q \), where the total number of processes is \( n = P \times Q \). When possible it is suggested to keep the same values for \( P \) and \( Q \), i.e., \( P = Q = \sqrt{n} \) [Petitet et al. 2012].

An approximation of the HPL execution time \( T \) that illustrates the cost of the dominant factors is [Petitet et al. 2012]:
\[
T = \frac{2}{3} \gamma_3 N^3 + \frac{\beta N^2(3P + Q)}{2PQ} + \frac{\alpha N(N_B + 1) \log P + P}{2NPQ} + \frac{\alpha N_N {N_B}^2}{N} \tag{5}
\]

**HPL performance.** HPL performance is the number of FLOPs divided by the execution time, and is expressed in FLOP/s. In order to simplify our mathematical formulas, we observe execution time per FLOP, which is the reciprocal for HPL performance.

If we assume \( P = Q = \sqrt{n} \) and analyze HPL execution time per FLOP by dividing (5) by (4), we have:
\[
\frac{1}{T_{\text{per FLOP}}} = \frac{3}{NP} \beta \sqrt{n} + \frac{3}{N} \alpha \left( \frac{1}{2} (N_B + 1) \log n + \sqrt{n} \right) \tag{6}
\]

Equation 6 describes the HPL execution time per FLOP as a function of the problem size \( N \). Per-core memory capacity \( m \) depends on the problem size \( N \) and the number of processes \( n \): \( m = \frac{10 N^2}{r} \). Therefore, the problem size that generates per-process memory capacity \( m \) when the HPL is executed on \( n \) processes can be computed as:
\[
N = \sqrt{\frac{r}{10}}. \tag{7}
\]

Equation 7 shows how the amount of memory changes when increasing the size of HPC systems.

11Problem size should be set to 80% of available memory [Petitet et al. 2012]. The \( N \times N \) coefficient matrix requires \( 8N^2 \) bytes, so the per-core memory capacity is \( \frac{100}{n} \times \frac{8N^2}{n} = \frac{10N^2}{n} \).
(number of cores). Dividing (7) by $\gamma_3$ to normalize relative to the lowest execution time with infinite memory gives the relative execution time per FLOP:

$$T_{rel\_per\_FLOP} = 1 + k_1 \frac{1}{\sqrt{m}} + (k_2 \sqrt{m} + k_3 \log n) \frac{1}{m}$$

(8)

Constants $k_1$, $k_2$, $k_3$ and $\gamma_3$ depend on the hardware platform, and for our platform we fit the constants according to the results from Figure 2. First we fit the constants $k_2$ and $k_3$, and then $k_1$ and $\gamma_3$ using linear regression. We get maximum error against experiments of 13%. Then, we analyze how much memory per core is needed to get close to ideal result with infinite memory, i.e., to reach a relative execution time per FLOP of $\varepsilon$. This we get by solving a quadratic equation:

$$(k_2 \sqrt{m} + k_3 \log n) \left( \frac{1}{\sqrt{m}} \right)^2 + k_1 \left( \frac{1}{\sqrt{m}} \right) + (1 - \varepsilon) = 0$$

(9)

The results for $\varepsilon$ values that contribute to 90%, 95% and 99% of ideal (infinite memory) HPL performance are explained in detail in Section 3.2. By taking the derivative of the solution to Equation 9, we find that, for any fixed target overhead $\varepsilon > 0$, increasing the number of cores $n$, always increases the memory per core, $m$. This shows that, as the total number of cores is increased, more memory per core is needed to achieve good execution time per FLOP, and therefore good HPL performance. This trend is confirmed by the experimental results in Section 3.1 and historical systems in Figure 3. Writing $k_1$, $k_2$ and $k_3$ in terms of $\alpha$ and $\beta$ then taking the derivatives with respect to $\alpha$ and $\beta$ shows that increasing interconnect latency or reducing interconnect bisection bandwidth also increase the memory per core for any fixed overhead $\varepsilon > 0$.

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